

27-750, A.D. Rollett

Due: Weds., 5th Feb., 2016.

Homework 3. Exercises with random orientations [100 points]

Revised 28 Jan 16.

1. [25 points]

Construct {100} and {110} pole figures for the Brass component, using the stereographic projection. You can find the expected result by looking back through the lecture notes.

Hints. (a) The points to be projected are on a sphere of unit radius, which ensures that each pole has unit length.

(b) The pole figure to be drawn is a circle of unit radius.

(c) Points on the southern hemisphere project outside the circle and should be ignored.

(d) It is probably easiest (and acceptable) to make a list of all the equivalent {100} and {110} poles, but the more sophisticated method is to generate all the equivalent points by applying crystal symmetry to a single example of each pole, before you apply the (inverse of the) orientation transformation. You should already have the set of symmetry operators

(e) It is a good idea to draw lines or arrows to indicate the positions of the x and y sample axes.

(f) To take account of sample symmetry, it should work to use the program/script that you developed in the last homework in which you applied sample symmetry. You should find that the output of that calculation gives you all the variants of the orientation. Also, if you leave the plot window open, subsequent plots will superimpose on the previous ones.

2. [25] Generate a set of random orientations and plot them in Euler space. Orient the plot (if 3D) so that you see either the 1st and 2nd angles or the 2nd and 3rd angles. Alternatively, make a 2D plot of the 1st versus the 2nd angle, or the 2nd versus the 3rd angle. Describe the variation in the density of points with respect to each angle.

Hints. Matlab provides a function “rand” that generates sets of random numbers.

“x=rand(200)” generates, e.g., a set of 200 random numbers (uniformly distributed over the interval 0 to 1).

There are many ways to generate random orientations and one method is to generate random values of the Euler angles. For the 1st and 3rd angles, one can simply multiply the randomly generated numbers by the desired range, say 360° (or 2 π). However, one must, for the 2nd angle, multiply the random number by 2, subtract 1 (so that it has the range -1 to +1), take the arc-cosine of the result and then (perhaps) multiply it by 180°/ π to get degrees).

3. [10] Use the procedure that you developed before to plot a {100} pole figure (or any other pole of your choice) of your random set. Comment on the distribution of points in the stereogram, especially as compared to the Euler space plot. This should help

convince you that the procedure above produces a uniform distribution on the sphere. You can try plotting with or without crystal symmetry (but it should not make any difference).

4. [10] Bin the points in 10° cells according to the 2^{nd} angle (Φ), i.e. in intervals 0-10, 10-20, 20-30 ... 80-90° (9 bins/cells in all). Plot a histogram (or 2D scatter plot) of the count in each bin versus the mid-point of the bin (5, 15, 25, ... 85°).

5. [10] Repeat the plot above but now divide each value by the total number of points, which gives you a volume fraction in each bin. On the same graph, plot the definite integral of $\sin(\Phi)$ for each cell, i.e. $\cos(0)-\cos(10)$, $\cos(10)-\cos(20)$, etc. This compares the theoretical volume fraction in each cell with a random sampling.

Hint. The values should be close unless you generated a very small number of random orientations. Note that this approach is effectively cell-edge binning (as opposed to cell-centered).

6. [10] Convert the values in each bin to intensities and plot them versus the mid-point angle. Hint. The procedure is described in the lecture notes. What line can you draw on the graph that is the theoretically expected value (for a truly random texture)? Hint: it should be a horizontal line.

7. [5] (a) What Miller indices are associated with each end of the “alpha fiber” in rolled fcc metals and what range of Euler angles are associated with this fiber? Hint: the charts developed by Bunge of Miller indices of points in Euler space should help you.

(b) [5] What Miller indices are associated with the “gamma fiber” in rolled bcc metals and what range of Euler angles are associated with this fiber?

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Q & A for this homework

Q. “In problem 2 when it asks for the $\{1\ 0\ 0\}$ pole figure, are we doing the same process (including the symmetries, namely) as in Hwk #2?”

A. Yes, you do indeed need to use the same application of symmetry as you did in Hw #2.